Fair Shares

Reporting Category  Number and Number Sense
Topic  Identifying the parts of a set
Primary SOL  2.3  The student will
   a) identify the parts of a set and/or region that represent fractions for halves, thirds, fourths, sixths, eighths, and tenths; and
   b) write the fractions.

Materials
   • Circular shaped counters
   • Paper plates
   • Fraction Story Problems (attached)
   • Chart paper
   • Markers

Vocabulary
   denominator, equivalent fraction, fair shares, fraction, numerator, unit fraction

Student/Teacher Actions (what students and teachers should be doing to facilitate learning)
1. Place students into five small groups, and give each group 12 circular shaped counters and 12 small paper plates. Explain that you will be reading a story problem (attached). As you read, they will use the counters and the plates to predict how the characters will solve the problem.
2. Display and read aloud the first story problem. Allow students to make predictions and then use their manipulatives to see if their predictions were correct. Discuss what happened to the set. Draw a pictorial representation or display a representation for the first division.
3. Give each group one of the remaining story problems to solve. Direct students in each group to discuss the problem, use the manipulatives to solve it, and then represent their solution on a piece of chart paper.
4. When groups have finished, have each group read their story problem aloud to the class and share their solution. Display each group’s chart.
5. After all groups have shared their story problems and solutions, discuss and compare what happened to the set of items being divided in each problem. Discuss the fair shares (equal-size portions) described in each problem. Explain that fractions are fair shares of a whole or a set.
6. Ask the students, “What do you notice happening to the fair shares as the denominator of the fraction gets larger?” Show students that when the set of 12 items was divided into halves, each share was $\frac{1}{2}$ of the 12 items, or a total of 6 items. When the set of 12 items
was divided into sixths, each share was \( \frac{1}{6} \) of the 12 items, or a total of 2 items. Have students look for the pattern, using the think-pair-share strategy. Students think about the patterns they see, talk about it with a partner, and then share as a whole class what they have discovered: the larger the denominator, the smaller the fair share.

**Assessment**

- **Questions**
  - Does a larger denominator mean that the fair share will be larger or smaller? Why?
  - Is it possible for a fraction with a large denominator to be larger than a fraction with a smaller denominator? For example, compare \( \frac{3}{4} \) with \( \frac{1}{2} \).
  - Compare the set model in the activity to the region/area model (fraction circles) of fractions. How are the models different? What do they have in common?
  - What would have happened if there had been a story problem in which five people had tried to share the 12 cookies? Is it possible to make fair shares? If not, what total number of cookies would have made it possible?

- **Journal/Writing Prompts**
  - Angie is playing with eight toy cars. She put them into groups of fourths. Draw pictures of what \( \frac{1}{4} \), \( \frac{2}{4} \), \( \frac{3}{4} \), and \( \frac{4}{4} \) of the cars look like. Explain how you know.
  - Logan has nine lollypops that he plans to share with four friends. Each friend will receive \( \frac{1}{4} \) of the lollypops. Draw a picture of each friend’s share. Is it possible to make fair shares? Explain why or why not.

- **Other**
  - Monitor groups as they are working on solving their story problems. Assist groups, as needed. When groups are sharing the solutions, listen for correct vocabulary usage and understanding of the concept.
  - Have student pairs or small groups complete a “3-2-1” by writing three things they learned about fractions, two ways that fractions are used in practical situations, and one thing that might be confusing about fractions.

**Extensions and Connections (for all students)**

- Have students investigate the relationship between skip counting and possible fair shares for a given number in a set. For example, a set of 10 items can be divided into 1, 2, 5 and 10 fair shares, but not into 3, 4, 6, 7, 8, or 9 fair shares. Give students an opportunity to predict numbers of fair shares for a given number in a set, based on skip counting patterns, and then to use manipulatives to confirm their predictions.

- Read a story about fractional concepts. Have students use manipulatives to model the fractions represented in the story.

- Have students write their own fraction story problems. Then, have them exchange their problems with partners to solve. Collect all story problems, and create a class book.
• Have students go on a “fraction hunt” for objects in the classroom, school building, or playground that represent or suggest fractions. If a digital camera is available, students can take pictures of the objects found and write the fractions on the pictures.

Strategies for Differentiation
• Have the students act out the story problems as they are read aloud to the class.
• Create a set of cards showing the solutions to the fraction story problems, and allow students to match solutions to the problems.
• Modify the fraction story problems to include picture cues for struggling readers.
Fraction Story Problems

**Story Problem 1**
Martin has 12 cookies. If he and his best friend Thomas share them equally, what fraction of the cookies does each boy get? How many cookies will be in each fractional share?

**Story Problem 2**
Devon has 12 cookies. He eats some of them at breakfast, some at lunch, and the rest of them at dinner. If he eats an equal number of cookies each time, what fraction of the cookies does he eat at each meal? How many cookies are in each fractional share?

**Story Problem 3**
Sarah has 12 cookies. If her family (Sarah, her mom, her dad, and her brother) shares them equally, what fraction of the cookies does each person get? How many cookies will be in each fractional share?

**Story Problem 4**
Mikah bought a box of 12 cookies for a party. If six friends show up, what fraction of the cookies will each friend get if they share them equally? How many cookies will be in each fractional share?

**Story Problem 5**
Victor has 12 cookies. He plans to eat one each day for the next 12 days. What fraction of cookies does he eat each day? How many cookies will be in each fractional share?

**Story Problem 6**
Mitch has 12 cookies. He accidentally drops the plate on the floor and his dog eats all of them. What fraction of cookies did the dog eat? How many cookies are in each fractional share?