## Just In Time Quick Check

**Standard of Learning (SOL) 4.15**

*Strand: Patterns, Functions, and Algebra*

The student will identify, describe, create, and extend patterns found in objects, pictures, numbers, and tables.

### Grade Level Skills:

- Identify and describe patterns, using words, objects, pictures, numbers, and tables.
- Create patterns using objects, pictures, numbers, and tables.
- Extend patterns, using objects, pictures, numbers, and tables.
- Solve practical problems that involve identifying, describing, and extending single-operation input and output rules, limited to addition, subtraction, and multiplication of whole numbers and addition and subtraction of fractions with like denominators of 12 or less.
- Identify the rule in a single-operation numerical pattern found in a list or table, limited to addition, subtraction, and multiplication of whole numbers.

### Supporting and Prerequisite SOL:

4.4b, 4.4d, 3.3b, 3.4d, 3.16, 2.6c, 2.16

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### Supporting Resources:

- **VDOE Mathematics Instructional Plans (MIPS)**
  - How Does the Pattern Grow? (Word) / (PDF Version)
- **VDOE Word Wall Cards: Grade 4** (Word) / (PDF)
  - Growing Patterns
  - In/Out Table
- **VDOE Algebra Readiness Remediation Plans**
  - Determine the Rule (Word) / (PDF)
  - Number Patterns and Rules (Word) / (PDF)
- **VDOE Algebra Readiness Formative Assessments**
  - 4.15 (Word) / (PDF)
- Desmos Activity
  - Diving into Growing Patterns
SOL 4.15 - Just in Time Quick Check

1. This list of numbers follows a pattern.
   1, 3, 9, 27, 81
   The pattern will continue to increase in the same way. What will be the next number in this pattern?

2. This pattern follows an increasing rule.
   \[ \frac{1}{4}, \frac{3}{4}, \frac{1}{4}, \frac{3}{4} \]
   The pattern will continue to increase in the same way. What will be the next number in this pattern? How do you know?

3. The first three figures in a pattern of candies are shown. The pattern of candies will continue to grow in the same way.
   a. Describe the rule to determine the increasing pattern of the candies.
   b. How many candies will be in the 5th figure of this pattern?
4. Ashley owns a dog training business. This table shows the number of dog treats Ashley has at the end of each week.

<table>
<thead>
<tr>
<th>Week</th>
<th>Number of Dog Treats</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>270</td>
</tr>
<tr>
<td>2</td>
<td>225</td>
</tr>
<tr>
<td>3</td>
<td>180</td>
</tr>
<tr>
<td>4</td>
<td>135</td>
</tr>
</tbody>
</table>

If the pattern shown in this table continues the same way, how many dog treats will Ashley have at the end of week 5?

5. The same rule is used on each input number in this table to create each output number.

<table>
<thead>
<tr>
<th>Input</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>12</td>
</tr>
<tr>
<td>5</td>
<td>30</td>
</tr>
<tr>
<td>?</td>
<td>42</td>
</tr>
<tr>
<td>9</td>
<td>54</td>
</tr>
<tr>
<td>12</td>
<td>72</td>
</tr>
</tbody>
</table>

What is the input number when the output number is 42?
SOL 4.15 - Just in Time Quick Check Teacher Notes
Common Errors/Misconceptions and their Possible Indications

1. This list of numbers follows a pattern.
   1, 3, 9, 27, 81
   
   The pattern will continue to increase in the same way. What will be the next number in this pattern?
   
   Some students may have the misconception that this pattern is adding two since 1+2=3, and some students may
   think the rule is +54 since 27 + 54 = 81. Other students may have difficulty understanding what a “rule” is. If
   students struggle with how to approach the problem, teachers may wish to have students think about what is
   happening with the numbers. Example questions: “Are the numbers increasing or decreasing?” “What
   mathematical operation would make this (increasing/decreasing) occur with numbers?” Once they are able to
   make the connection that increasing numbers are a result of addition or multiplication, students can progress to
   analyze the pattern. Ask the students “How is the pattern changing?” “How do you move from 1 to 3? 3 to 9?
   What operation can we apply so the move is the same between every number?” Students may benefit from the
   use of manipulatives to model how the pattern is changing. Exposure to a variety of patterns using different
   objects, pictures, and numbers would be helpful to students.

2. This pattern follows an increasing rule.
   \[
   \frac{1}{4}, \frac{3}{4}, 1, \frac{1}{4}, 1 \frac{3}{4}
   \]
   The pattern will continue to increase in the same way. What will be the next number in this pattern? How do
   you know?
   
   Some students may have difficulty understanding what value is added to each fraction to obtain the next
   fraction. Students may think since the pattern begins with \( \frac{1}{4} \), that \( \frac{1}{4} \) is the amount of increase. Many students
   struggle to understand they are adding a different amount than what they began with. If students have trouble
   thinking about the fraction relationship, they may benefit from the use of fraction manipulatives (fraction bars or
   fraction strips) or a number line with increments of \( \frac{1}{4} \) to determine the increasing change between each fraction.
   A review of SOL 3.2, counting fractional parts, may help some students make connections between the fractional
   parts and the pattern.

3. The first three figures in a pattern of candies are shown. The pattern of candies will continue to grow in the
   same way.
   
   Figure 1
   Figure 2
   Figure 3
   
   a. Describe the rule to determine the increasing pattern of the candies.
   b. How many candies will be in the 5th figure of this pattern?
Some students may have trouble describing the rule in their own words. Encourage students to look at the initial section of the pattern and then focus on the section of the pattern that is growing. Students can then look at the next figure to see if the growing pattern continues. Encourage students to use a strategy such as sentence frames to structure their thinking as they describe the rule.

Other students may have difficulty determining the growing pattern presented as a picture. Students may benefit from using manipulatives to replicate the pattern. Replicating the pattern with concrete materials will help students make the connection to a numerical representation. Students should be encouraged to write the number of candies for each set of triangles underneath the picture. This will help students think about the pattern numerically, and aid them in extending the pattern.

Some students will recognize the pattern is increasing by one triangle each time, and these students will think the answer is 5 because there will be 5 triangles in the fifth figure. Encourage students to think about what information has been provided in the problem. The focus in this problem is on the increasing pattern of the candies and how many candies will be in the 5th figure.

4. Ashley owns a dog training business. This table shows the number of dog treats Ashley has at the end of each week.

<table>
<thead>
<tr>
<th>Week</th>
<th>Number of Dog Treats</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
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<td>3</td>
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</tr>
<tr>
<td>4</td>
<td>135</td>
</tr>
</tbody>
</table>

If the pattern shown in this table continues the same way, how many dog treats will Ashley have at the end of week 5?

A common error is assuming that all patterns are increasing. Students with this misconception would add on to the Week 4 amount rather than subtracting from it. Encourage students to look at the numbers and focus on whether they are increasing or decreasing. Once students determine that the numbers are decreasing, have them think about which operations might cause the numbers to decrease.

Another common error is assuming that the rule is based on the smallest number in the pattern which would result in students subtracting and determining that Week 5 is 0. Students would benefit from practice finding a rule and checking multiple spots in the table to determine if the rule applies to every change in the table. These students may struggle to understand that the rule in a pattern should apply to every iteration of the pattern.

Lead students to discuss what is happening to the numbers in the table and make the connection that decreasing number of dog treats means that the operation/rule must be subtraction or division. Providing concrete examples with context for students to think about will help them come to this conclusion. If students have difficulty analyzing and determining whether the pattern is increasing vs. decreasing, this may indicate that students need to develop a conceptual understanding of increasing and decreasing using operations and then make this connection to tables.
5. The same rule is used on each input number in this table to create each output number.

<table>
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<tbody>
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</tr>
</tbody>
</table>

What is the input number when the output number is 42?

A common error is focusing on the numbers in the output column and predicting the next output. Students with this misconception might add on to the last output without considering the input column. Encourage students to look for the relationship between each input and output number to help them find the rule for this input-output table. Having students write out the number sentence for each row, emphasizing the rule as part of the number sentence, may help students see the relationship between the input column and the output column (ex: \(2 \times 6 = 12\); \(5 \times 6 = 30\); \(9 \times 6 = 54\)).

Another common error is incorrectly applying the rule for the input-output table. As students look at the relationship between the input and output columns, they may correctly determine the rule, but then forget that they are looking for the input number. Students with this misconception may apply the rule to the output number rather than using missing number thinking or inverse relationships to determine the input number. Encourage students to look at the inverse relationships demonstrated in the table. For example, if the rule involves a multiplication rule for the input number, students could also explore applying a division rule to the output number and discussing the inverse relationships of those number sentences.